



Drift wave nature of the Weakly Coherent Mode on ASDEX Upgrade

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author list of U. Stroth *et al* 2022 *Nucl. Fusion* **62** 042006

I-mode: Improved energy confinement mode

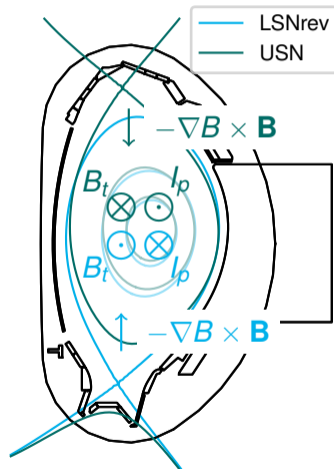
ELM-free confinement regime

“Recipe” for I-mode:

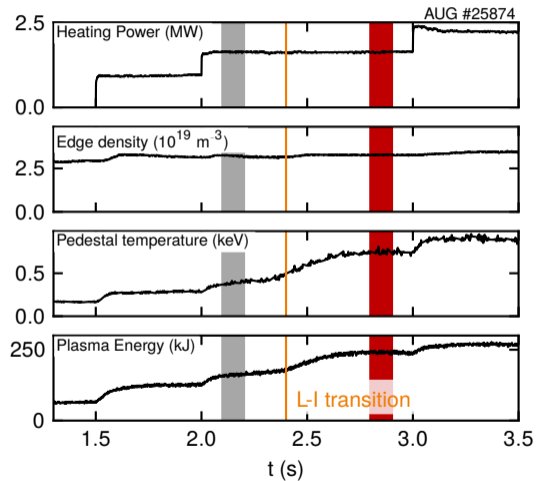
- Strong enough heating
- Unfavorable magnetic configuration

Configurations at ASDEX Upgrade:

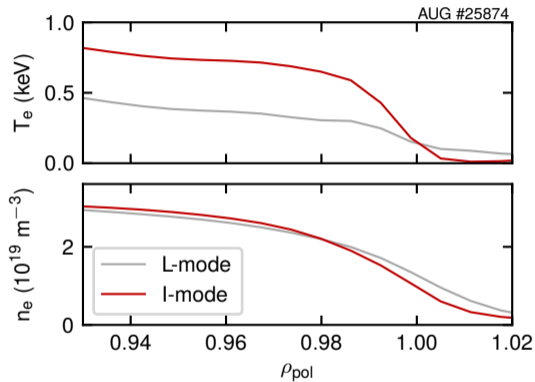
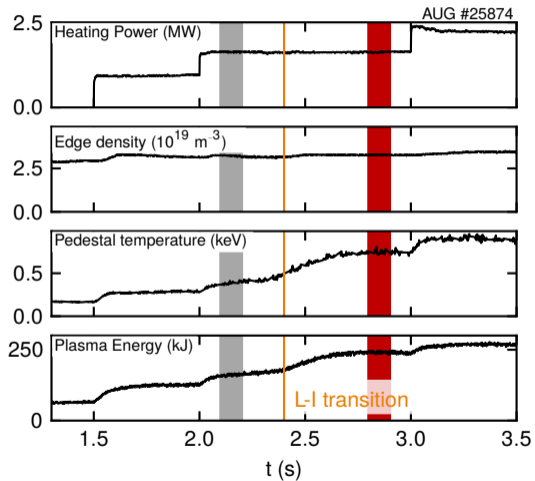
- **LSNrev**: Lower Single Null with reversed I_p , B_t
- **USN**: Upper Single Null



I-mode: Improved energy confinement mode

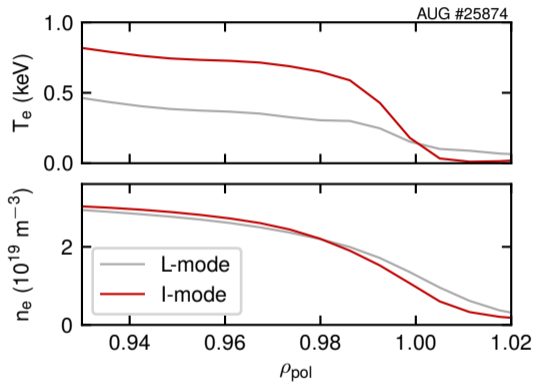
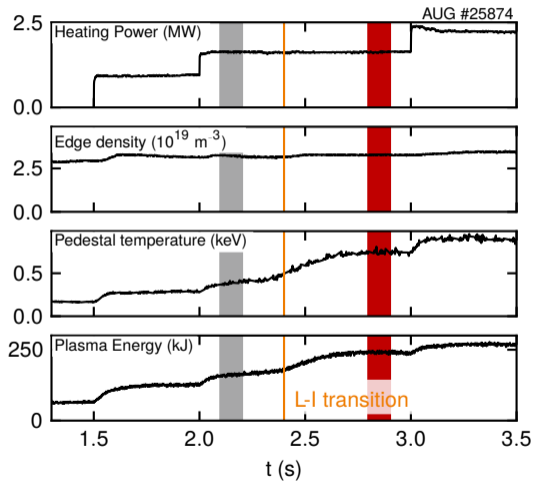


I-mode: Improved energy confinement mode



Pedestal only in temperature

I-mode: Improved energy confinement mode



Pedestal only in temperature

Unusual, unlike other regimes

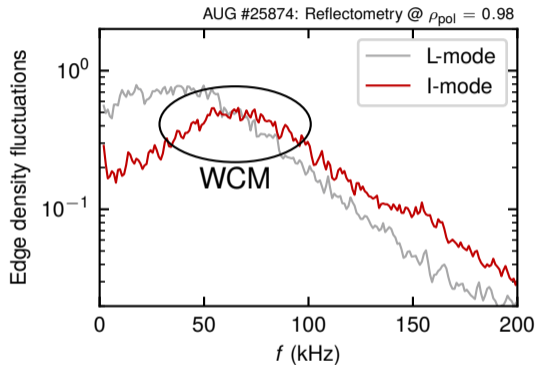
Weakly Coherent Mode

- Reduction in low frequency turbulence
- Appearance of weakly coherent mode (WCM)

WCM often suspected to cause unusual edge transport in I-mode

Origin of the WCM?

WCM responsible for I-mode?



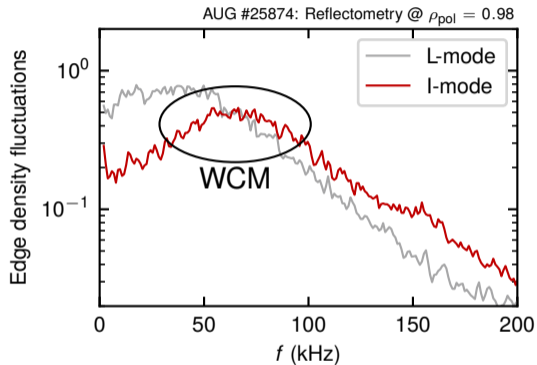
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Underlying instability?

Instability	Drive	Propagation	Scale	$\alpha_{\phi, \tilde{p}}$
IPM	J_{\parallel}	n.p.	$k_{\theta} \rho_s \ll 0.1$	
(I-R)BM	$\nabla \rho$	n.p.	$k_{\theta} \rho_s < 0.1$	$\pi/2$
KBM	$\nabla T_{e,i}$	i dia.	$k_{\theta} \rho_s \sim 0.1$	$\pi/2$
MTM	∇T_e	e dia.	$k_{\theta} \rho_s \sim 0.1$	0
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[Manz 2018 Habil.]

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[Manz 2018 Habil.]

Underlying instability?

Instability

IPM
 (I-R)BM
 KBM
 MTM
 DW
 TEM
 ITG
 ETG

Drive

difficult

Propagation

n.p.
 n.p.
 i dia.
 e dia.
 e dia.
 e dia.
 i dia.
 e dia.

Scale

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\Rightarrow Look at phase velocity: $v_{\text{lab, WCM}} = v_{E \times B} + v_{\text{ph, WCM}}$

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⇒ Look at phase velocity:

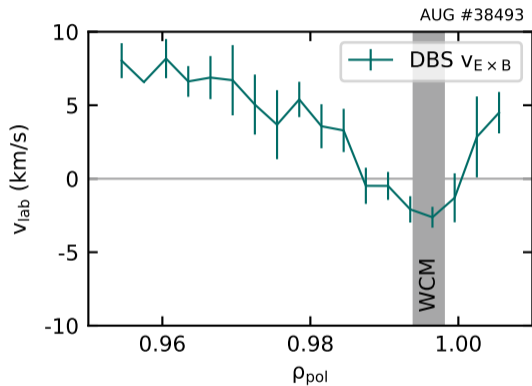
$$\underbrace{v_{\text{lab, WCM}}}_{\text{Helium Beam @ } 0.5 \text{ cm}^{-1}} = \underbrace{v_{E \times B}}_{\text{Doppler @ } 10 \text{ cm}^{-1}} + v_{\text{ph, WCM}}$$

[Manz 2018 Habil.]

Velocity profiles

- Experimentally:

$$V_{\text{phase}} = V_{\text{lab,WCM}} - V_{E \times B}$$

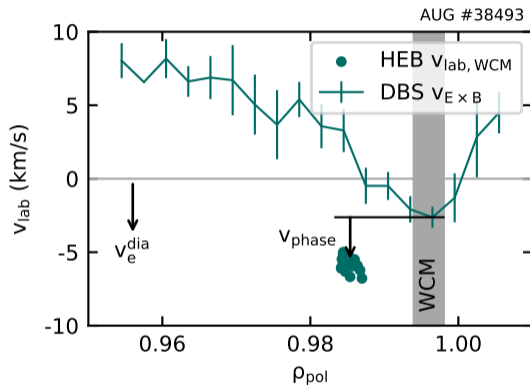


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- WCM phase velocity in electron-diamagnetic drift direction

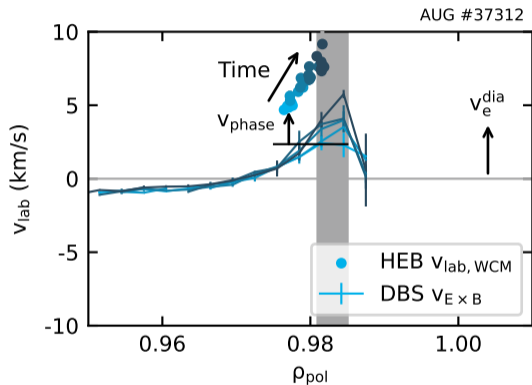


Velocity profiles

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- Found in [USN](#) and [LSNrev](#)



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Remaining instabilities "drift-wave-like", as in simulations

Liu et al 2016 Phys. Plasmas 23 120703

Manz et al 2020 Nucl. Fusion 60 096011

Lang et al 2022 Nucl. Fusion 62 086018

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Comparison to experimental phase velocity

- Typical drift wave phase velocity:

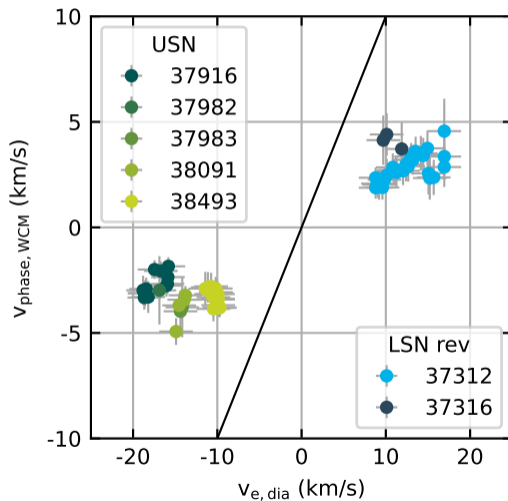
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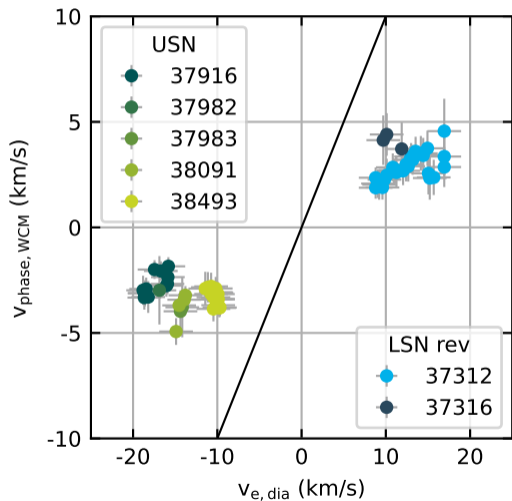
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- Poor agreement

But: theory can help us!



Excursion: our current understanding of I-mode

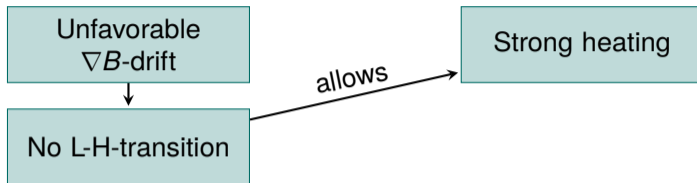


Unfavorable
 ∇B -drift

Strong heating

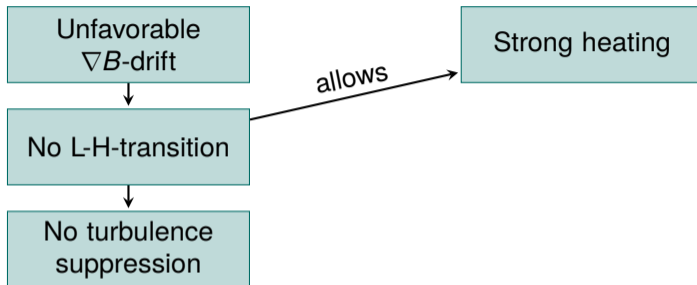
Manz et al 2020 Nucl. Fusion

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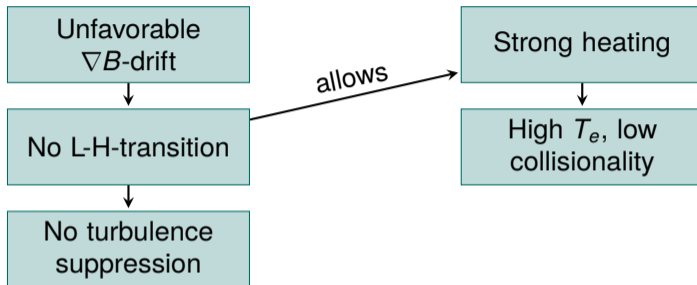
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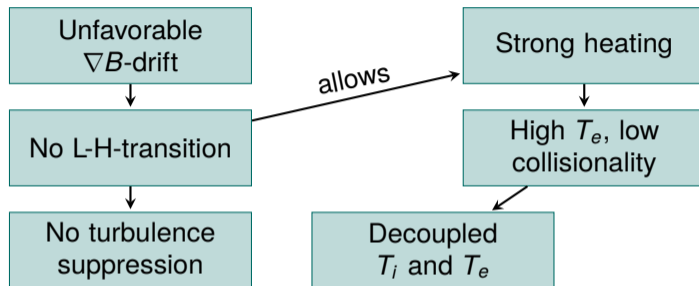
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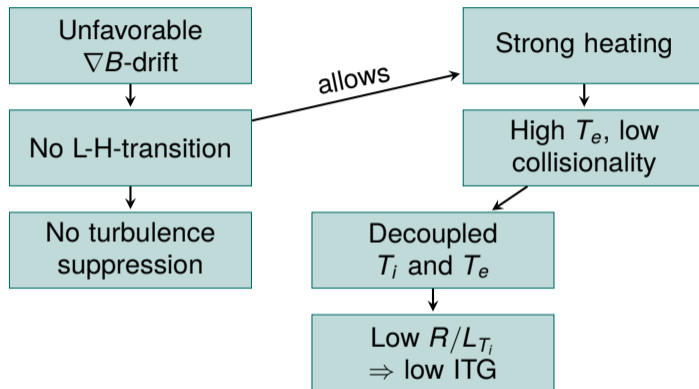
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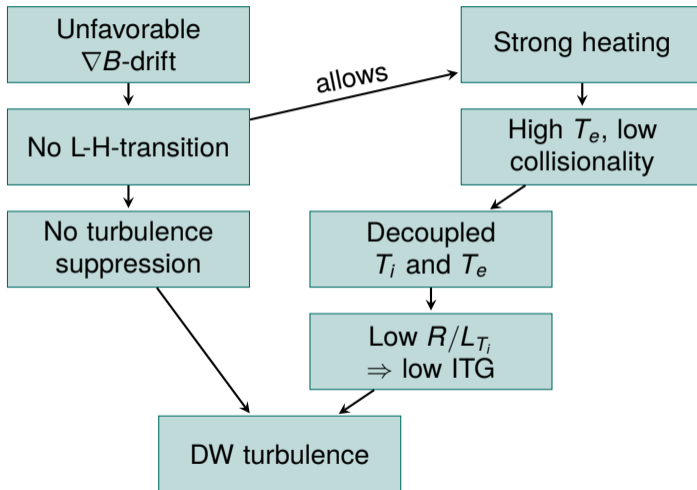
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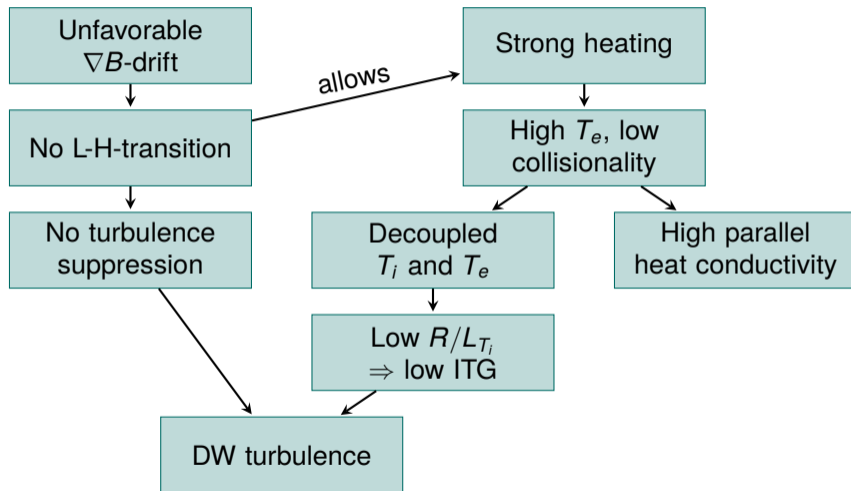
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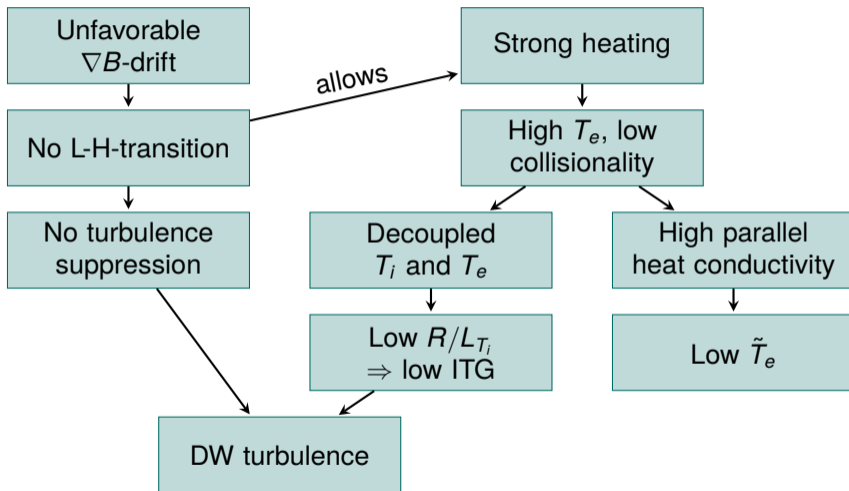
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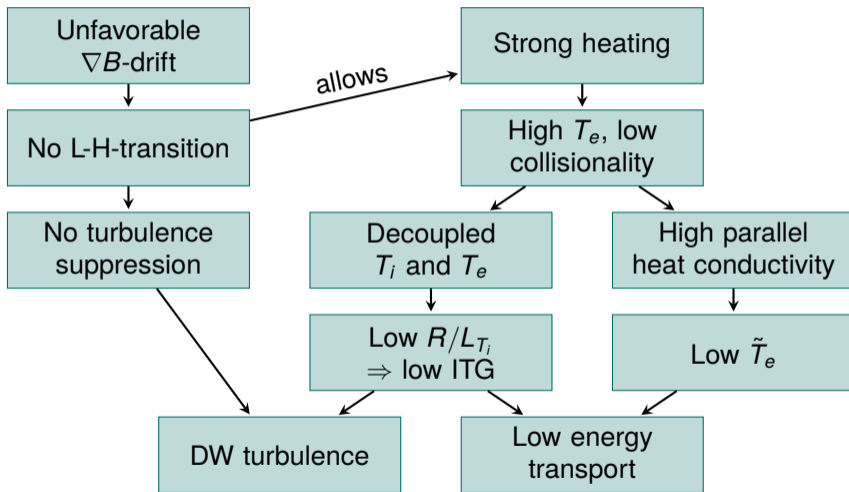
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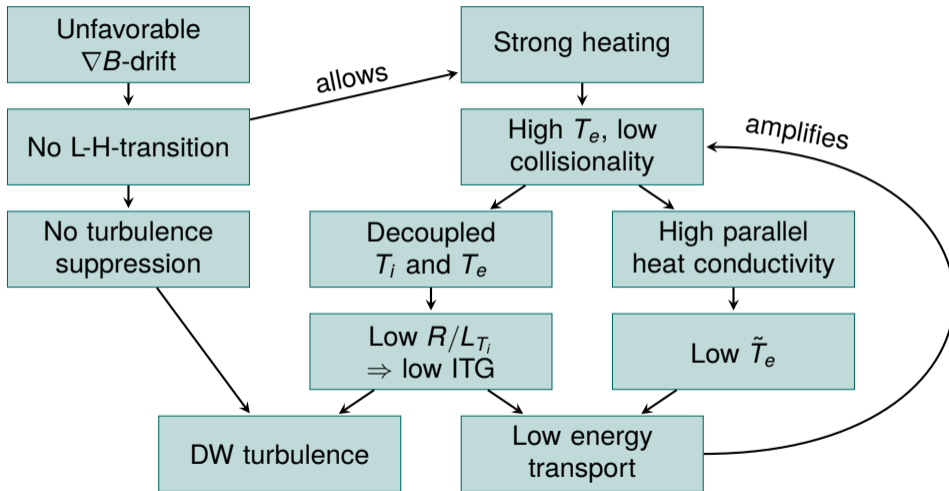
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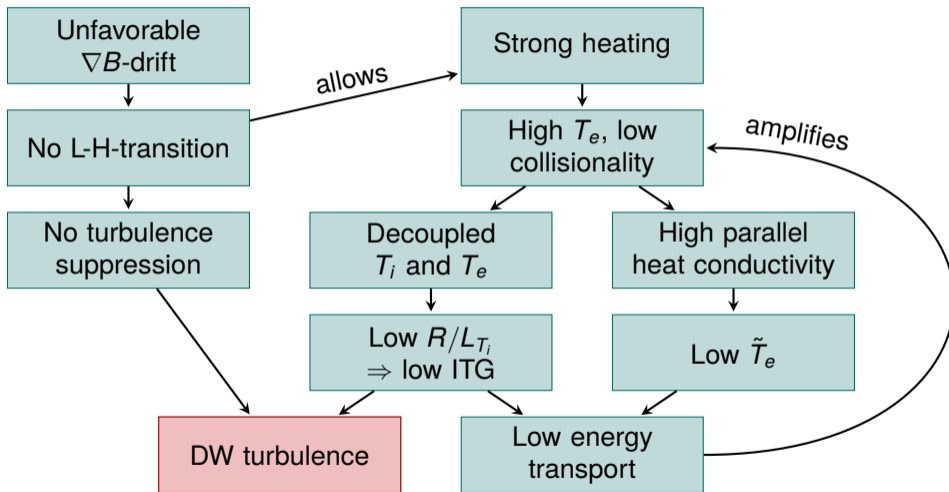
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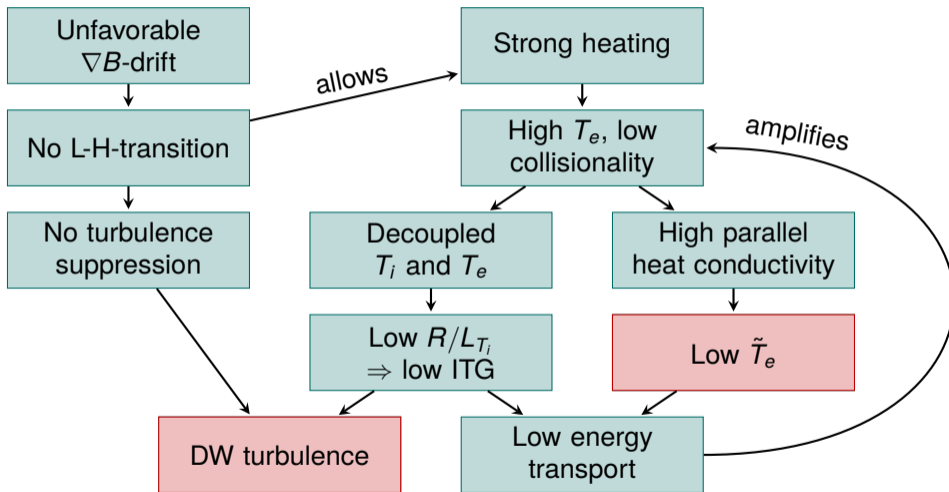
Manz et al 2020 Nucl. Fusion

Excursion: our current understanding of I-mode



Manz et al 2020 Nucl. Fusion

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Manz et al 2020 Nucl. Fusion

Impact of temperature fluctuations

- Boltzmann's law in drift wave theory:

$$\frac{e\tilde{\Phi}}{T_e} = \frac{\tilde{n}}{n_0} + \frac{\tilde{T}_e}{T_{e,0}}$$

- Drift wave phase velocity:

$$v_{\text{ph,DW}} = \frac{T_e}{eB} \left(\frac{1}{L_n} + \frac{1}{L_T} \right)$$

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Negligible temperature fluctuations decrease v_{ph}

Comparison to experimental phase velocity II



- Drift wave phase velocity without \tilde{T}_e :

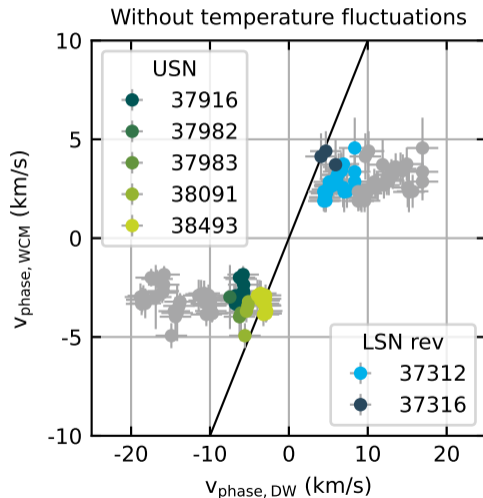
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- Drift wave phase velocity without \tilde{T}_e :

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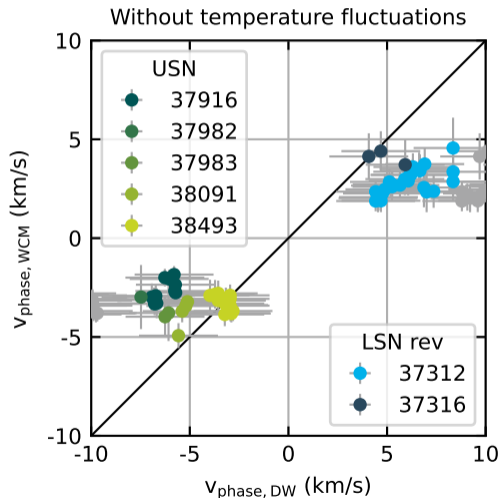


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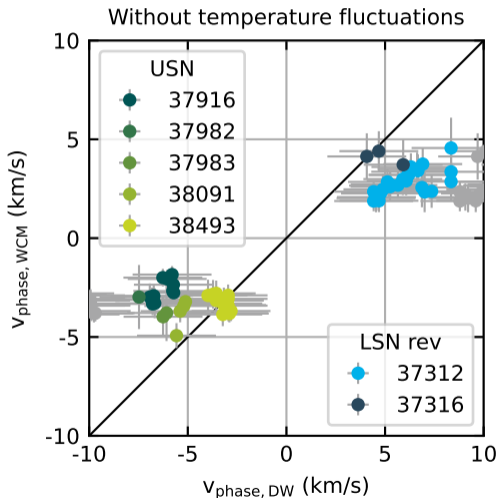
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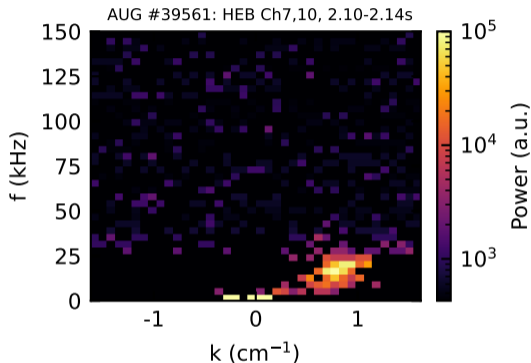
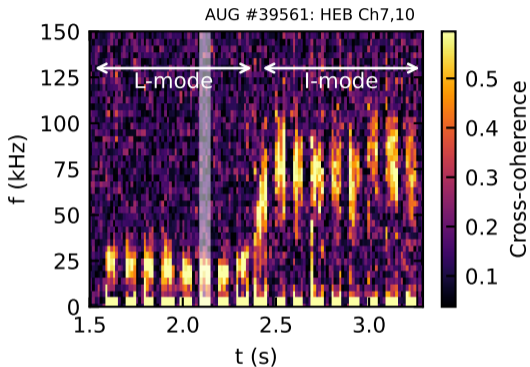
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Various uncertainties:

- Instability type (DW, TEM, MTM)
- Cross-phases $\alpha_{\phi, \tilde{n}}$ and $\alpha_{\phi, \tilde{T}_e}$
- v_{phase} in Doppler



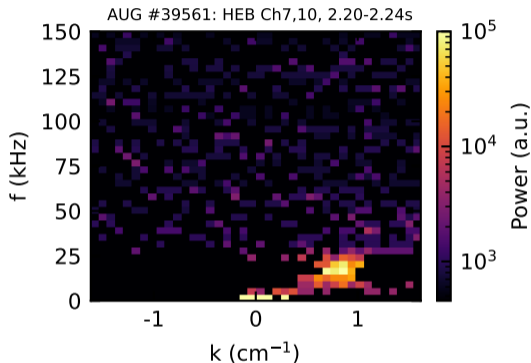
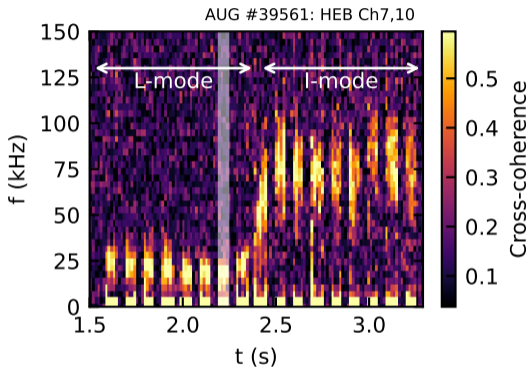
Our current understanding of WCM



L-mode WCM visible in coherence diagnostic

Happel et al 2019 NME
Bielajew et al 2022 Phys. Plasmas

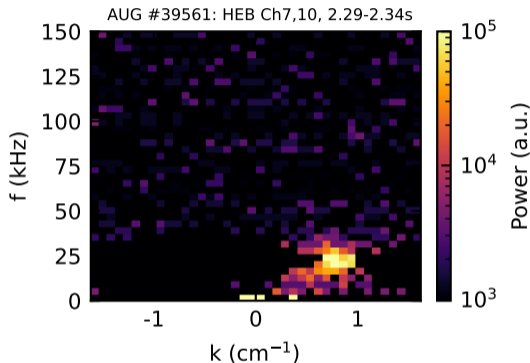
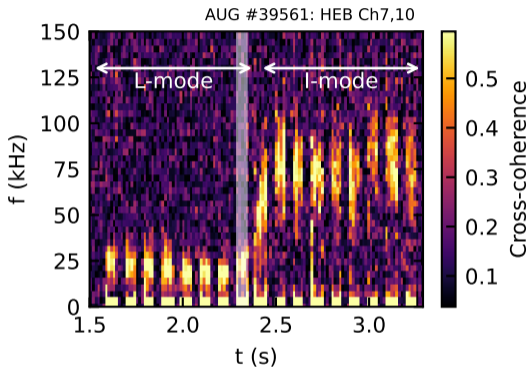
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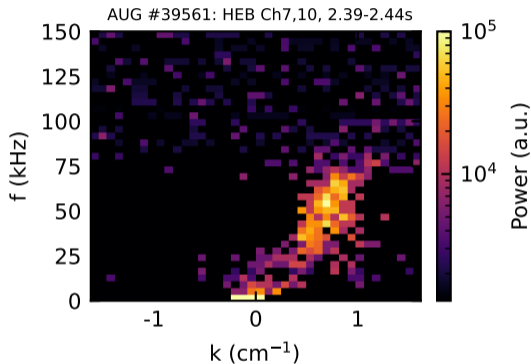
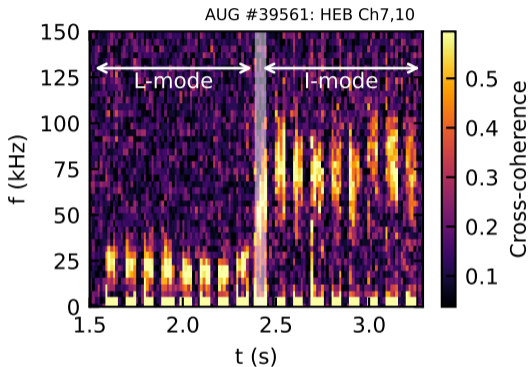
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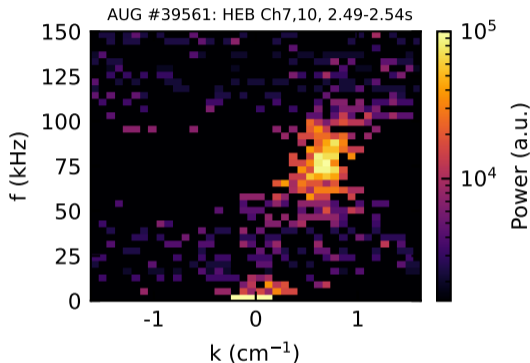
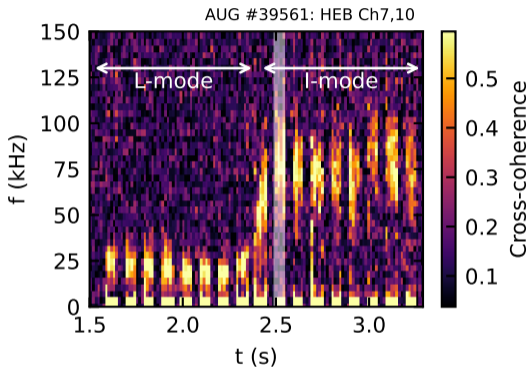
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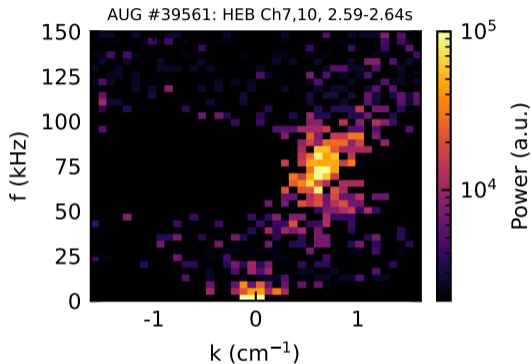
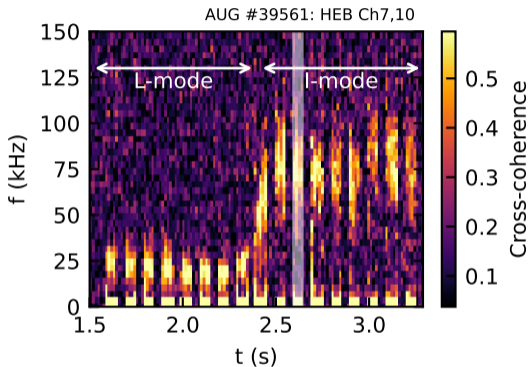
Our current understanding of WCM



L-mode WCM visible in coherence diagnostic

Happel et al 2019 NME
Bielajew et al 2022 Phys. Plasmas

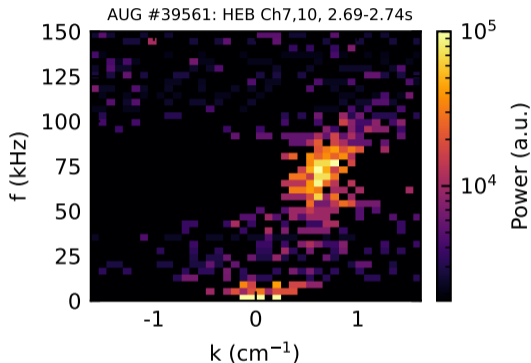
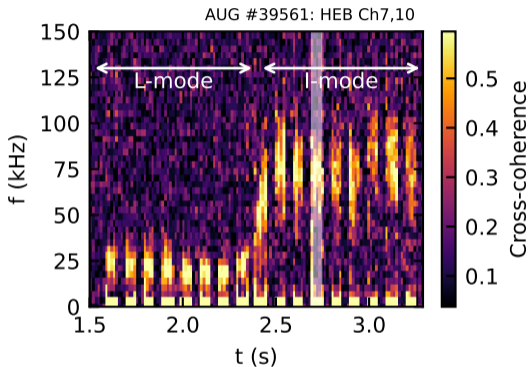
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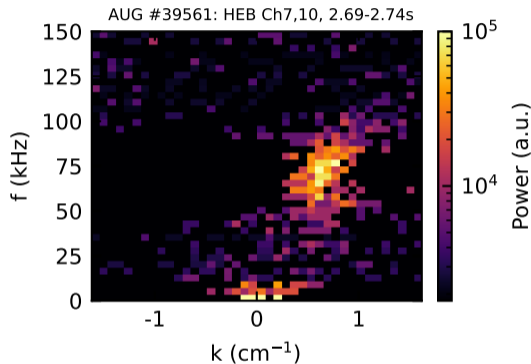
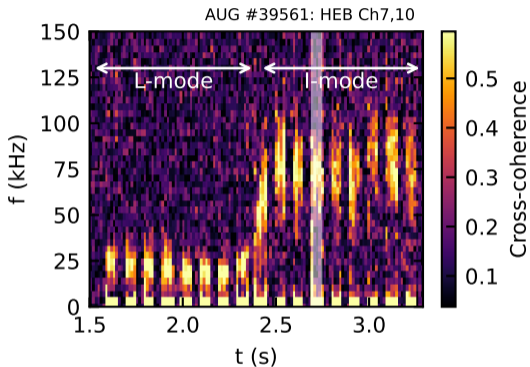
Our current understanding of WCM



L-mode WCM visible in coherence diagnostic

Happel et al 2019 NME
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Our current understanding of WCM



$$\underbrace{f_{\text{WCM}}}_{\nearrow \text{ at L-I-transition}} = \frac{1}{2\pi} \underbrace{k_{\text{WCM}}}_{\searrow} \left(\underbrace{V_{E \times B}}_{\nearrow} + \underbrace{V_{\text{ph,WCM}}}_{\nearrow} \right)$$

Prediction for WCM frequency

- Only I-mode plasma considered (yet)
- Use fixed k_{WCM} to estimate f_{WCM} :

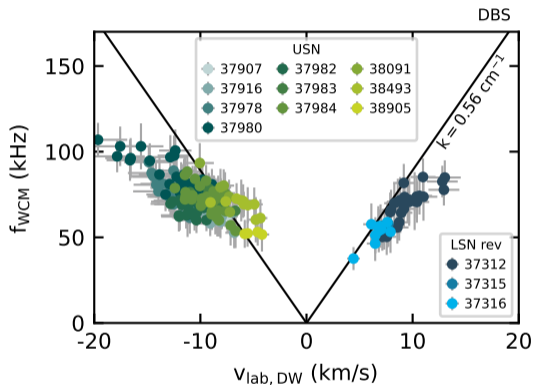
$$f_{\text{WCM}} = \frac{1}{2\pi} k_{\text{WCM}} \underbrace{(v_{E \times B} + v_{\text{ph, DW}})}_{v_{\text{lab, DW}}}$$

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- Predicts f_{WCM} in most cases

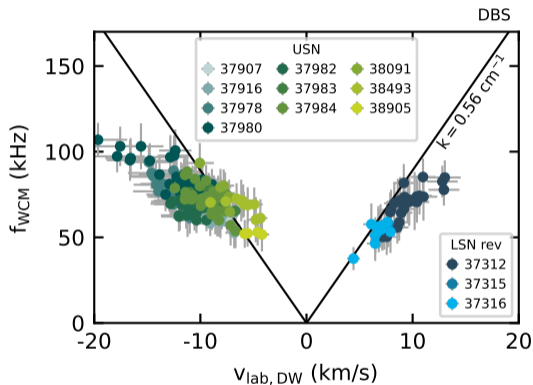


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- Predicts f_{WCM} in most cases
- L-I-transition: future work



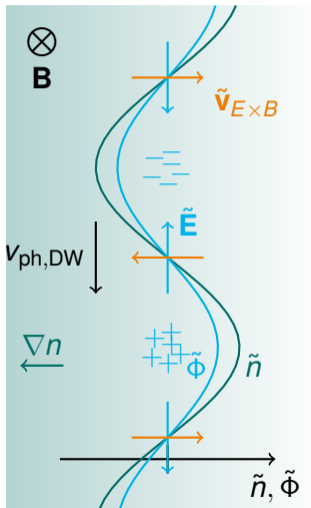
Summary

- WCM matches drift wave with low \tilde{T}_e
- Consistent with current understanding of I-mode
- WCM appears in I-mode due to acceleration in lab frame
- Transport caused by WCM not directly measured

Outlook:

- Hopefully measurements with Langmuir probes
- Simulations with GRILLIX
- Comparison with C-Mod data envisioned

Ideal drift wave



- For simplest drift wave: $\nabla n, \mathbf{B}, \tilde{n}$
- Electrons react fast to density perturbation:

$$\frac{\tilde{n}}{n_0} = \frac{e\tilde{\Phi}}{T_e}$$

- Cross-phase between \tilde{n} and $\tilde{\Phi}$ zero
- Electric and magnetic field $\Rightarrow \mathbf{v}_{E \times B}$
- Perturbation propagates:

$$v_{ph,DW} = \frac{T_e}{eL_n B}$$

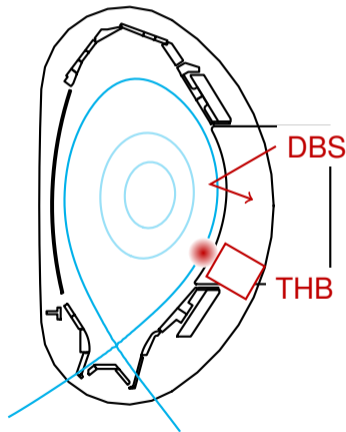
Diagnostics

Edge diagnostics used here:

- Thermal Helium Beam (THB)
- Doppler Back-Scattering (DBS)

Procedure (not covered here):

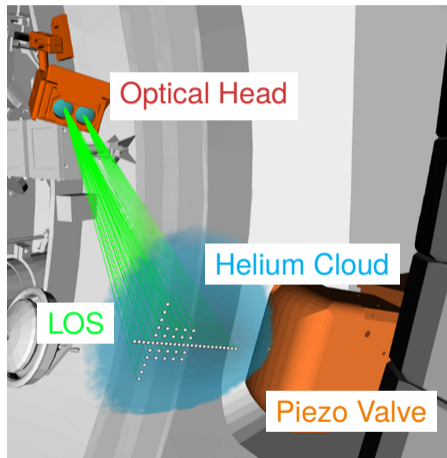
- Setup up database of I-mode shots
- Automatically scan diagnostics for WCM
- Filter database to remove noisy data



Diagnostics: Thermal Helium Beam

- Spectroscopic diagnostic
- Small cloud of helium puffed
- Measure line radiation at many lines-of-sight
- Cross-coherence
 $\Rightarrow f_{\text{WCM}}, k_{\text{WCM}}$
 $\Rightarrow v_{\text{lab,WCM}}$
- Measures at WCM scales
 $(k_{\text{WCM}} \approx 0.5 \text{ cm}^{-1})$:

$$v_{\text{lab,WCM}} = v_{E \times B} + \underbrace{v_{\text{ph}}(k_{\text{WCM}})}_{v_{\text{ph,WCM}}}$$

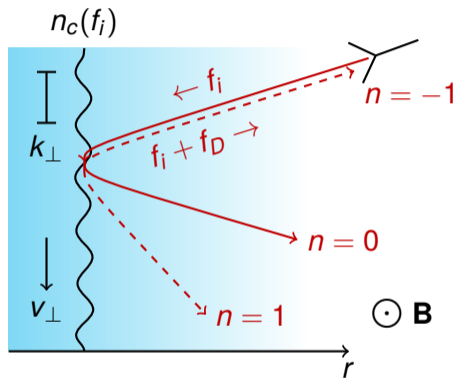


Diagnostics: Doppler Back-Scattering

- Microwave beam scatters at turbulence
- Signal returns Doppler-shifted
- Measures at small scales ($k_{\perp} \approx 10 \text{ cm}^{-1}$):

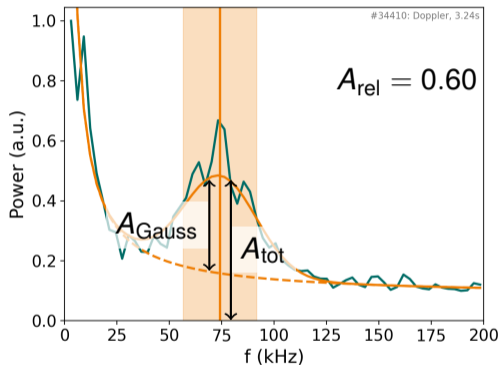
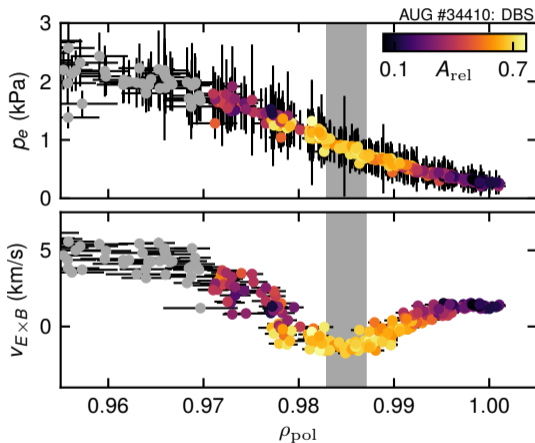
$$v_{\perp} = v_{E \times B} + \underbrace{v_{\text{ph}}(k_{\perp})}_{=0 \text{ at } k_{\perp}}$$

- Incident frequency can be hopped \Rightarrow Radial scan
- Indirectly picks up f_{WCM}



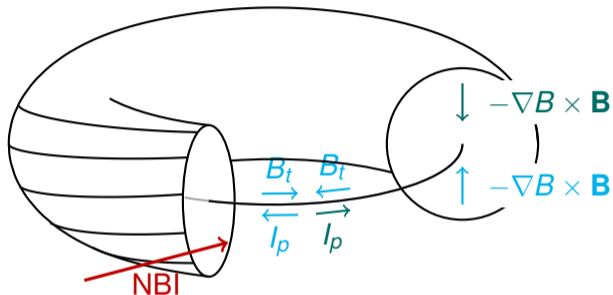
k_{\perp} given by Bragg's law

Experimental approach: Mode localization



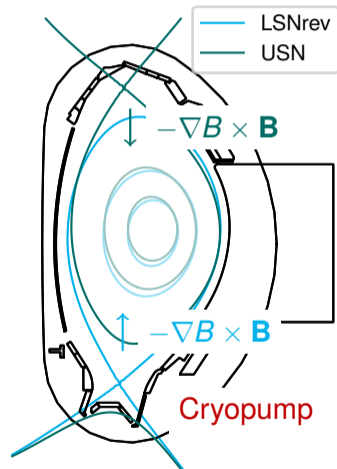
$$A_{rel} = A_{Gauss}/A_{tot}$$

I-mode: Magnetic configurations

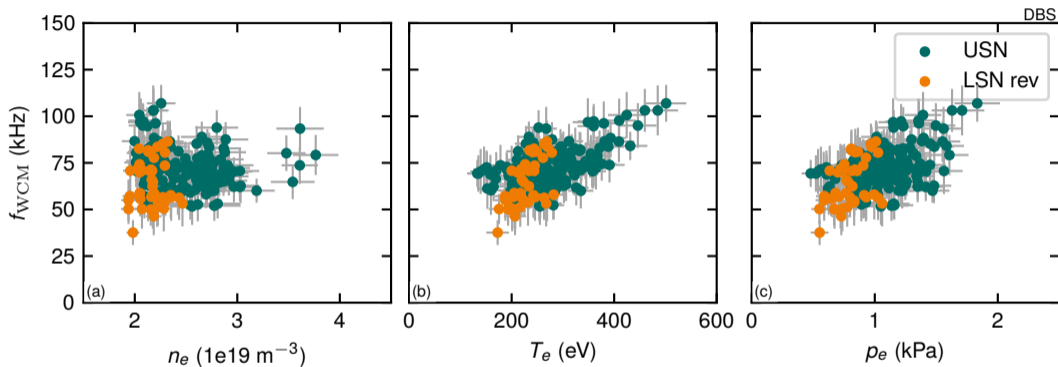


Configurations used for I-mode: **USN** and **LSNrev**

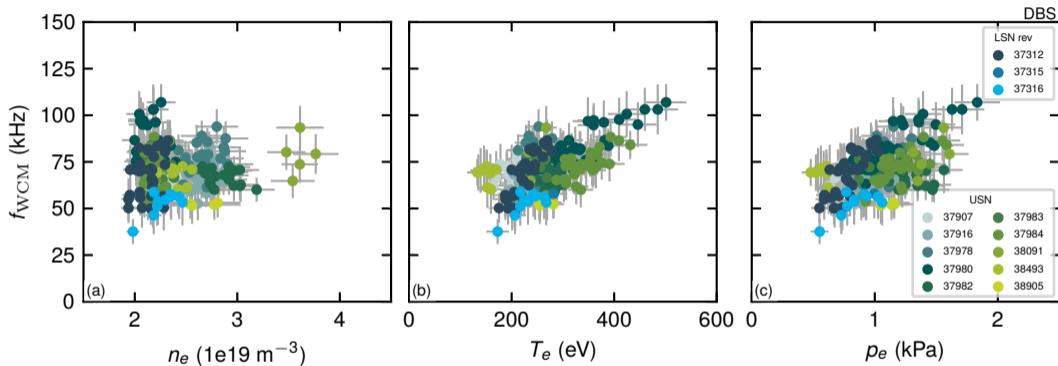
Main differences: NBI and divertor pumping



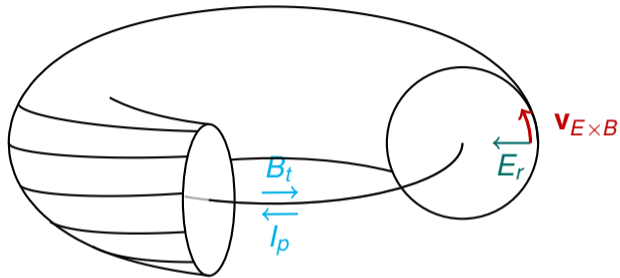
WCM frequency scaling



WCM frequency scaling



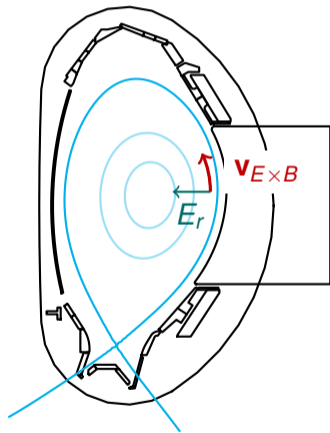
Plasma velocity



Complicated radial electric field E_r

Plasma rotates with $v_{E \times B} = \frac{\mathbf{E} \times \mathbf{B}}{B^2}$

⇒ “Plasma frame”

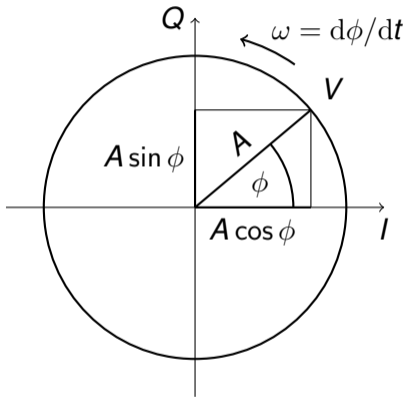


Heterodyne signal detection

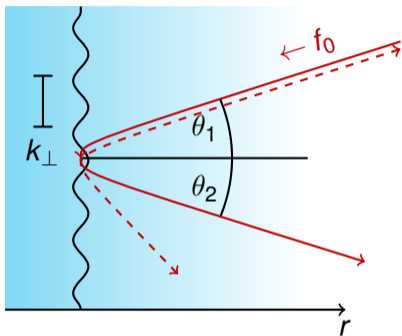
- Mix signal with reference and with 90° phase-shifted reference
- Down-conversion to remove emitted frequency ω_0
- Phase and amplitude of reflected wave detected
- Complex values obtained

$$V = A \cos \phi + i A \sin \phi = A e^{i\phi}$$

- WCM strongest in spectrum of $d\phi/dt$

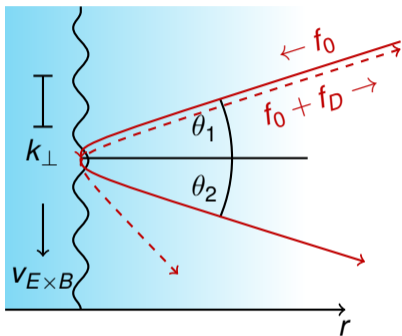


Doppler Back-Scattering (DBS)



- Microwave scattering at specific turbulence scale k_{\perp}

Doppler Back-Scattering (DBS)

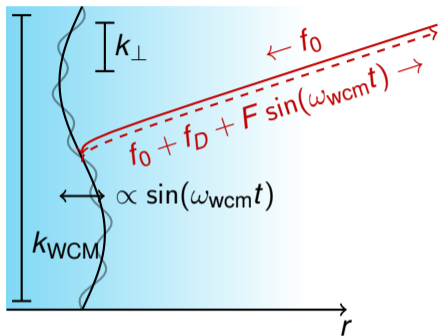


- Microwave scattering at specific turbulence scale k_{\perp}
- Outgoing beam Doppler shifted

$$f_D = v_{E \times B} \cdot k_{\perp} / 2\pi$$

- Measure plasma velocity $v_{E \times B}$

Doppler Back-Scattering (DBS)



- Microwave scattering at specific turbulence scale k_{\perp}
- Outgoing beam Doppler shifted

$$f_D = v_{E \times B} \cdot k_{\perp} / 2\pi$$

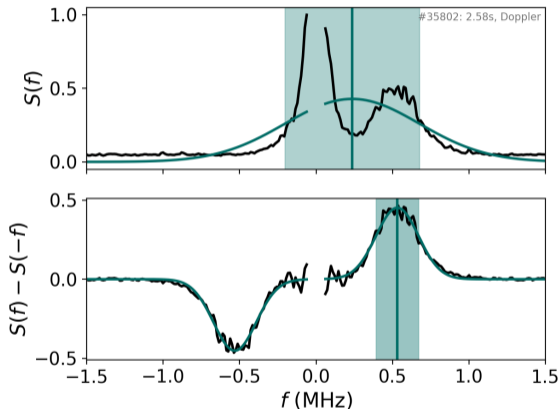
- Measure plasma velocity $v_{E \times B}$
- Indirectly picks up f_{WCM} , but cannot measure $v_{lab, WCM}$

Doppler Reflectometry

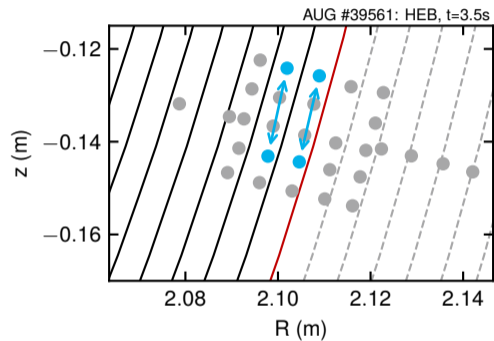
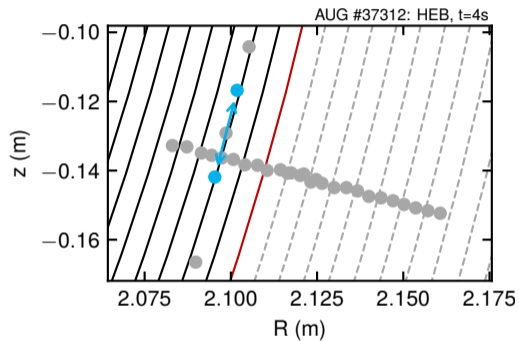
Fitting the Doppler shift f_D :

- Simple case: Gaussian peak
- Sometimes a strong 0th-order reflection present
- Use asymmetric part of the spectrum in these cases
- Use empiric criteria to detect failed fits

Does not always work automated,
requires manual adjustments



THB: LOS setup



Helium Beam

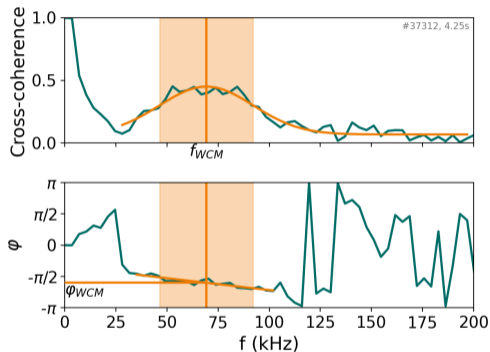
- Single channel relatively noisy
- Use multiple lines of sight for correlation
- Cross-correlation yields both coherence and phase
- Phase can be used to get k_{wcm}

$$k_{wcm} = \varphi_{wcm}/d$$

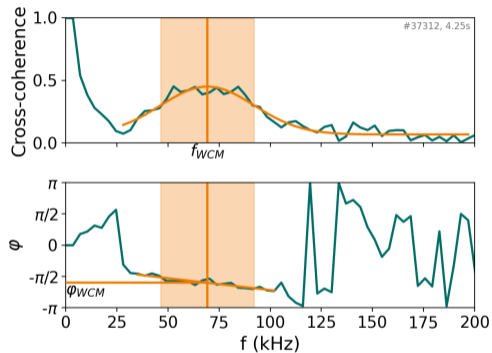
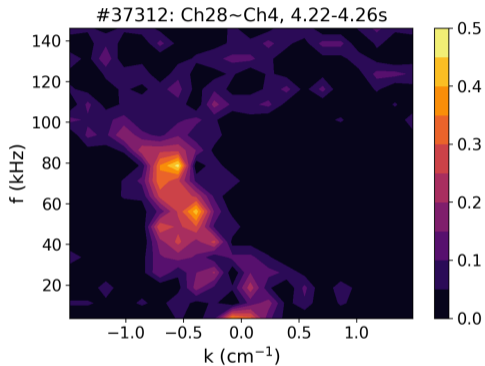
with distance d between LOS

- Calculate v_{wcm} with

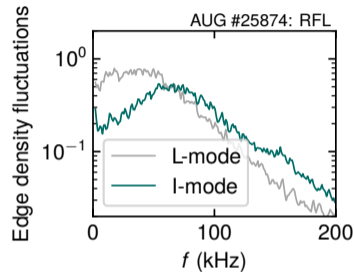
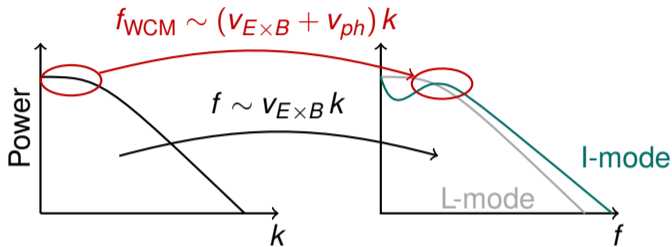
$$v_{wcm} = 2\pi f_{wcm}/k_{wcm}$$



Helium Beam



Discussion



k-spectrum could be the same in L- and I-mode

Phase velocity shifts WCM in f-spectrum