



# Experimental validation of momentum transport theory in the core of a tokamak plasma



C. F. B. Zimmermann, R. M. McDermott, C. Angioni, B. P. Duval, R. Dux,  
E. Fable, T. Luda, T. Pütterich, A. Salmi, U. Stroth, T. Tala, G. Tardini,  
and the ASDEX Upgrade Experimental Team

27<sup>th</sup> Joint EU-US Transport Task Force, 14<sup>th</sup> September 2023



This work has been carried out within the framework of the EUROfusion Consortium, funded by the European Union via the Euratom Research and Training Programme (Grant Agreement No 101052200 — EUROfusion). Views and opinions expressed are however those of the author(s) only and do not necessarily reflect those of the European Union or the European Commission. Neither the European Union nor the European Commission can be held responsible for them.

# Motivation



- Understanding of momentum transport **crucial to predict toroidal plasma rotation**, which
  - impacts impurity transport (see talks from F. Reimold and D. Fajardo)
  - stabilizes turbulence via  $E \times B$  shear → **influences confinement**
  - **provides stability** against MHD events → **avoids disruptions**
- **No fully validated theoretical model** for momentum transport available  
→ no predictive capability for rotation profiles of a future reactor
- **Momentum transport studies are challenging** due to a third transport mechanism  
→ Strong assumptions or **simplifications usually made** in previous exp. works
- To be presented: method to **assess** the momentum **transport coefficients purely from experimental data** and **validate theoretical predictions**

# Outline



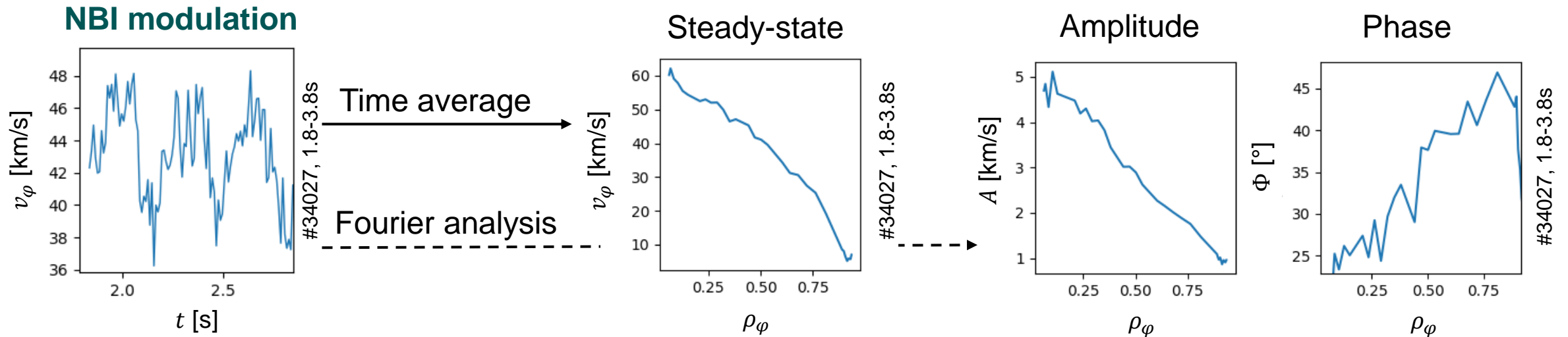
- Introduction
- **Background** of the Methodology: Equations and Modeling
- Comparison of **Gyrokinetic Predictions and Experimental Results**
- **Parameter and Isotope Dependence** of Momentum Transport
- Summary and Outlook

# Momentum Transport Equation

$$m \frac{\partial}{\partial t} n R v_\varphi = - \frac{1}{V'} \frac{\partial}{\partial \rho} V' \left[ \begin{array}{c} \text{Flux} \\ \Gamma_\varphi \end{array} \right] + \begin{array}{c} \text{NBI} \\ S_{NBI} \end{array}$$

$$\Gamma_\varphi = - m n R \left( \begin{array}{c} \text{Diffusion} \\ \chi_\varphi \frac{\partial v_\varphi}{\partial \rho} \end{array} - \begin{array}{c} \text{Conv.} \\ V_c v_\varphi \end{array} \right) + \begin{array}{c} \text{Res. stress} \\ \Pi_{RS} \end{array}$$

→ Problem underconstrained in a steady-state analysis

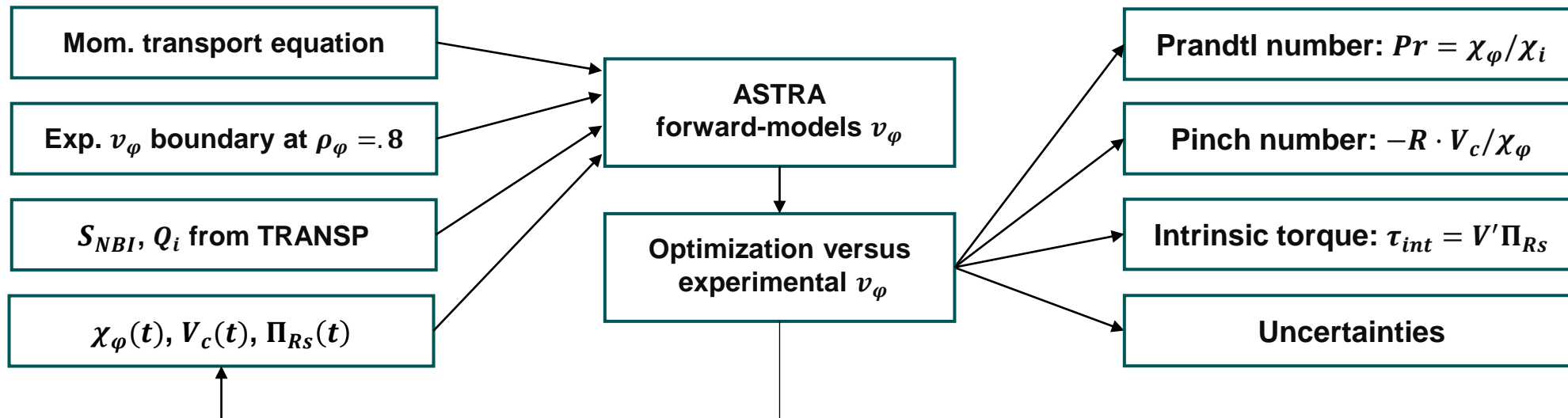


→ Problem constrained if modulation of turbulence can be compensated

# Momentum Transport Modeling

$$m \frac{\partial}{\partial t} n R v_\varphi = - \frac{1}{V'} \frac{\partial}{\partial \rho} V' \left[ \begin{array}{c} \text{Flux} \\ \Gamma_\varphi \end{array} + \begin{array}{c} \text{NBI} \\ S_{NBI} \end{array} \right]$$

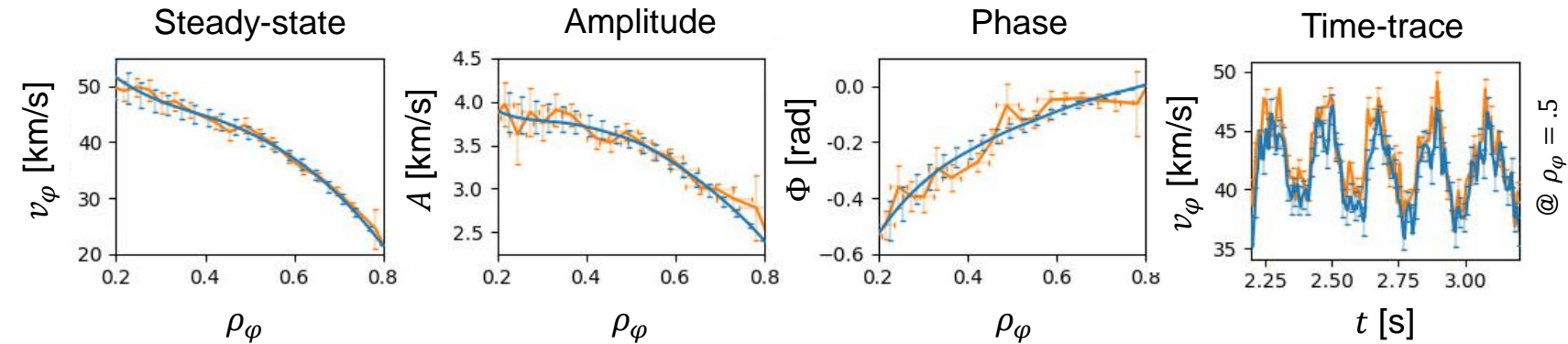
$$\Gamma_\varphi = -mnR \left( \begin{array}{c} \text{Diffusion} \\ \chi_\varphi \frac{\partial v_\varphi}{\partial \rho} \end{array} - \begin{array}{c} \text{Conv.} \\ V_c v_\varphi \end{array} \right) + \begin{array}{c} \text{Res. stress} \\ \Pi_{RS} \end{array}$$



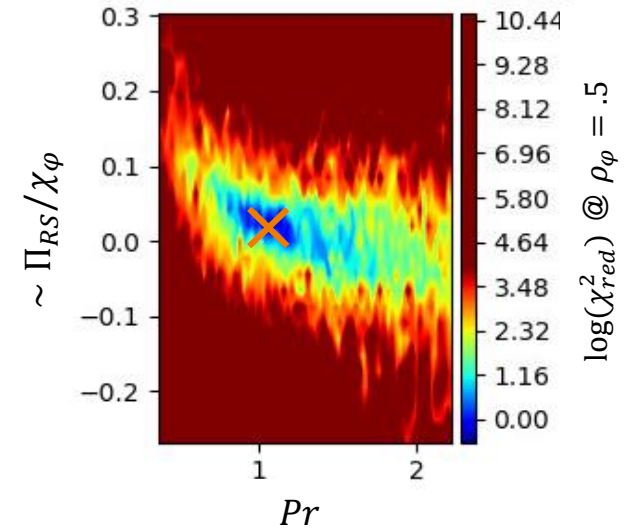
- First model to **retain time dependencies** (via  $\chi_i$ ) in all transport coefficients and channels
- Concept has been **validated on a broad set of discharges** [Zimmermann et al. PPCF. 64. 2022]

# Fitting of the reference case #40076 at 1.8-4.2s (ELMy H-mode)

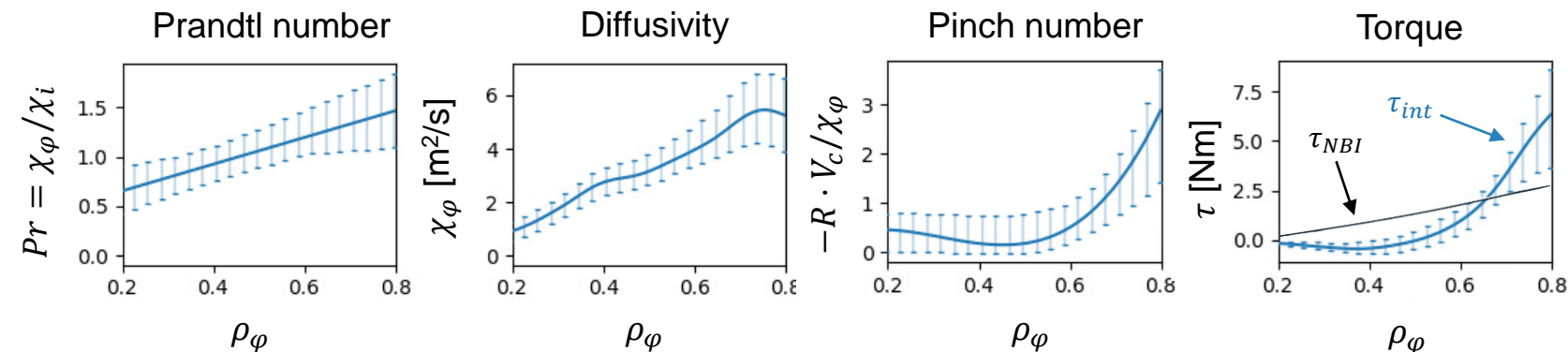
Experimental data vs. successful ASTRA modelling



Colormap of the parameter space



Transport Coefficients:



→ unique solution obtained

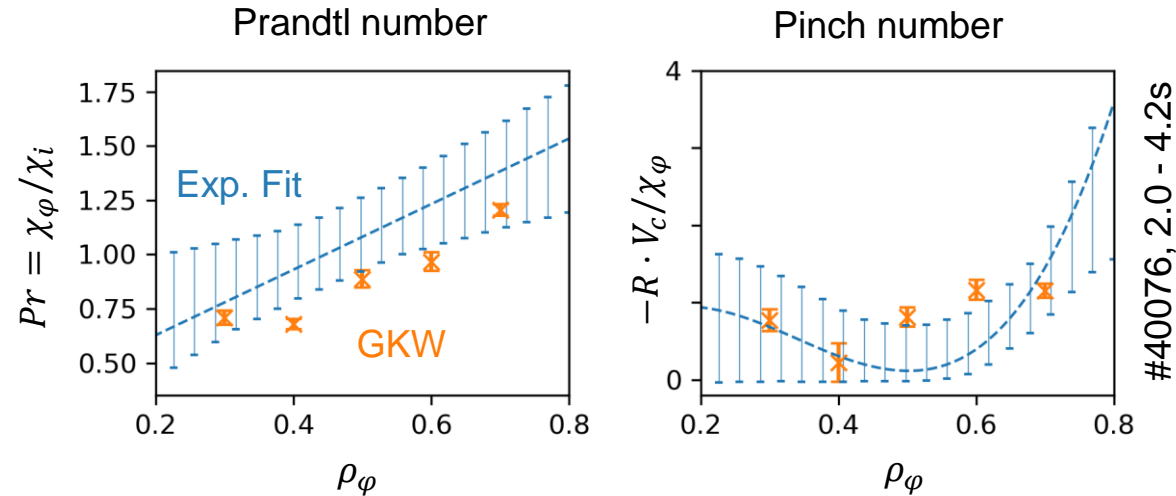
# Outline



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# Validation of Gyrokinetic Predictions

- Performed quasi-linear, local gyrokinetic calculations via GKW



- Coefficients are predicted to be stable despite modulation,  $\chi_i$  time dependence valid
- Good agreement of Gyrokinetic Predictions and Experimental Results for ITG dominated plasma
  - First time to quantitatively validate this kind of theoretical predictions
  - Retaining time dependencies is crucial to obtain best solution

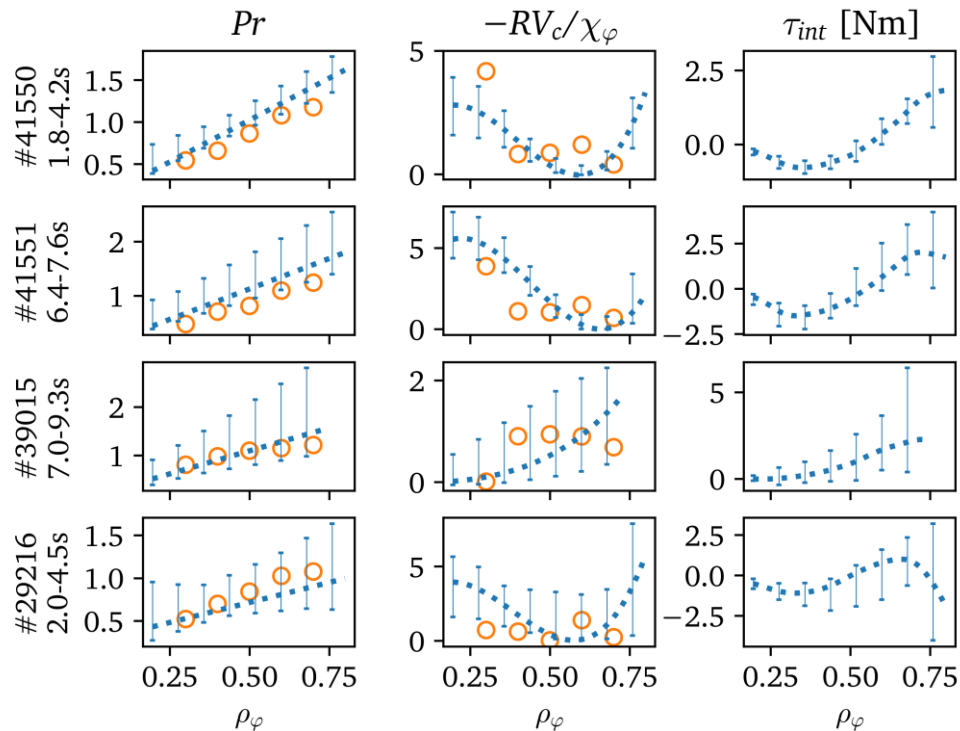


# Parameter Dependence of Momentum Transport

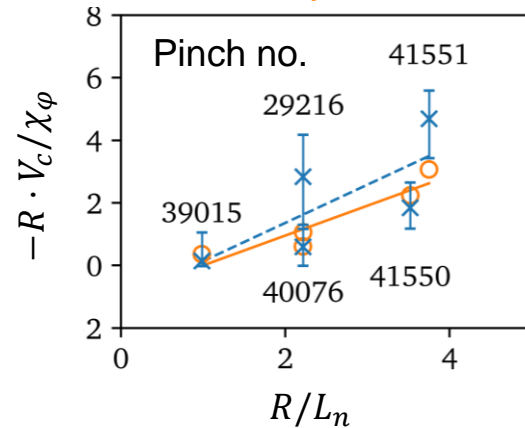
[Zimmermann et al. NF Letter. 2023. Submitted.]

Compared ITG dominated discharges with variation in plasma current, density, and density gradient:

Experiment vs. GKW prediction

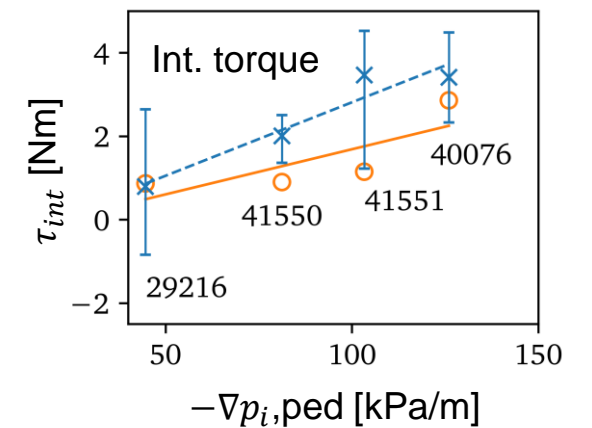


Experiment at  $\rho_\phi = .35$  vs. GKW prediction



→ Coriolis pinch, deformation of the eigenfunction &  $k_{||}$

Experiment at  $\rho_\phi = .7$  vs. Stolfus-Dueck model



→ deeper  $E_r$  well, smaller turbulence decay length?

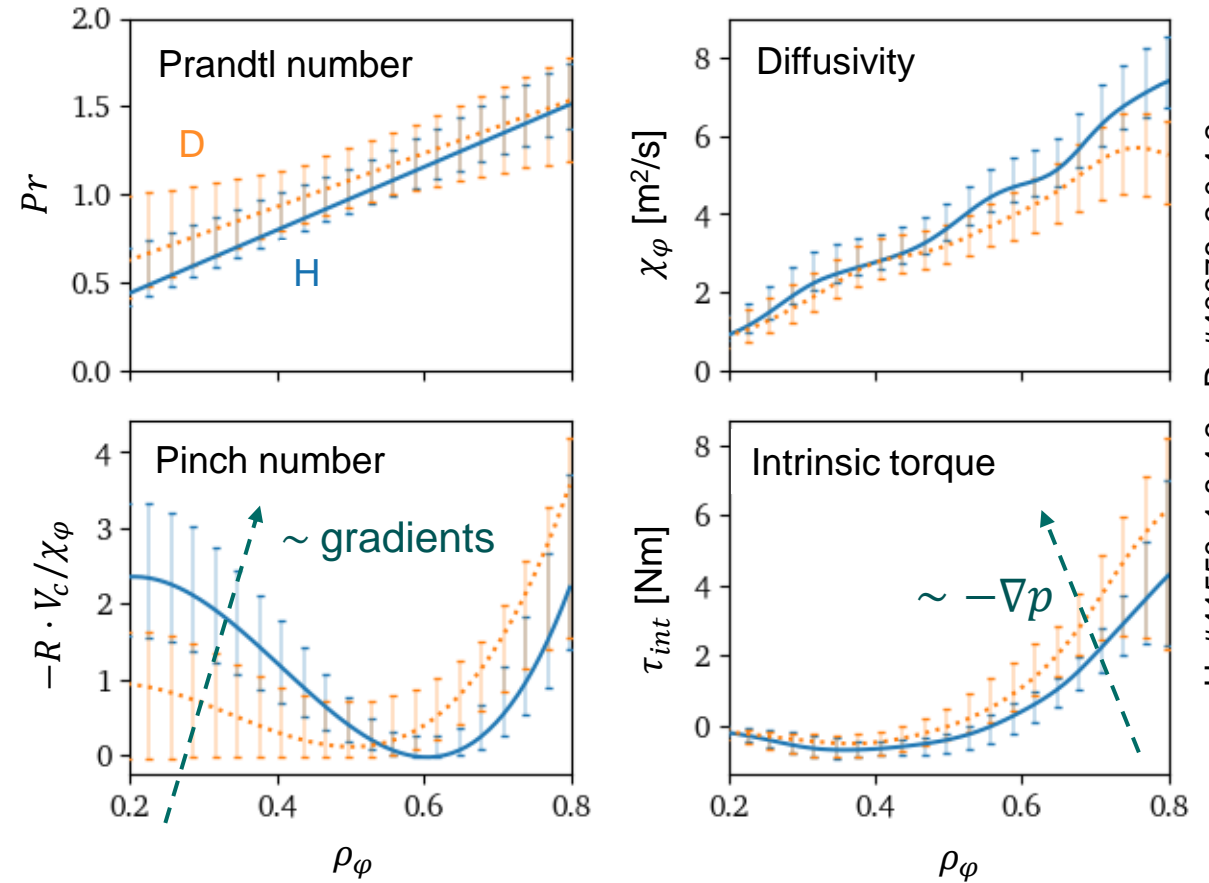
→ Technique opens the door to further theory validation and physics-based parameter scalings

# Isotope Dependence of Momentum Transport

[Zimmermann et al. NF. 63. 2023]

- Comparison of hydrogen and deuterium plasma
- Matched fluxes, dimensionless parameters, and heat transport to isolate isotope dependence
- Theory predicts negligible isotope dependence
- Very similar transport coefficients assessed:
- Variation of  $\tau_{int} \sim -\nabla p$  at edge,

$$\frac{-RV_c}{\chi_\phi} \sim \text{gradients in core}$$



H: #41550, 1.8-4.2s; D: #40076, 2.0-4.2s

→ Increases confidence when applying theory to other main ion species and mixtures

# Summary and Outlook



- Developed a code framework to extract momentum transport coefficients purely from experimental data
- First methodology to disentangle all three momentum fluxes simultaneously, key requirement is retaining the time dependencies
- Validated gyrokinetic predictions for ITG dominated plasmas, studied theory scalings on convection, intrinsic torque, and isotope dependence
- Expand this validation to more discharges ( $\rightarrow$  TEM), compare to a GKW data base
- Apply this technique to other tokamaks as JET and KSTAR to analyze  $\rho_*$  dependence (A. Kirjasuo)
- Develop physics-based scaling laws, to be used for example in integrated modeling approaches

# References



- Momentum transport equation: [Fable. PPCF. 2017]
- GKW code: [Peeters. CPC. 2009]
- ASTRA code: [Pereverzev. MPI. 2002]
- Coriolis pinch: [Peeters. PRL. 2007]
- NUBEAM/TRANSP code: [Beslau. PPPL. 2018] [Pankin. CPC. 2004]
- Prandtl number: [Strintzi. PoP. 2008]
- Stoltzfus-Dueck model: [Stoltzfus-Dueck. PRL. 2012]
- IMEP: [Luda. NF. 2021]